

**Visvesvaraya Technological University, Belagavi**

**MODEL QUESTION PAPER**

**5<sup>th</sup> Semester, B.E (CBCS) EC/TC**

**Course: 15EC52 - Digital Signal processing**

**Time: 3 Hours**

**Max Marks: 80**

**Note: (i) Answer Five full questions selecting any one full question from each Module.**

**(ii) Question on a topic of a Module may appear in either its 1<sup>st</sup> or 2<sup>nd</sup> question.**

<b>Module 1</b>			
1	(a)	Explain the frequency domain sampling and reconstruction of discrete time signals.	8
	(b)	The first five points of the eight point DFT of a real valued sequence are {0.25, 0.125-j0.3018, 0, 0.125-j0.0518, 0}. Determine the remaining three points.	3
	(c)	Determine the circular convolution of the sequences, $x_1(n) = \{1,2,3,1\}$ , $x_2(n)=\{4,3,2,2\}$ using time domain approach.	5
<b>OR</b>			
2	(a)	Obtain the relationship of DFT with the Z-transform.	5
	(b)	Show that the multiplication of two DFTs leads to circular convolution of respective time sequences.	7
	(c)	Consider a finite duration sequence $x(n) = \{0,1,2,3,4\}$ . (i) Determine the sequence $y(n)$ with six point DFT $Y(k) = \text{Real}[X(k)]$ (ii) Determine the sequence $v(n)$ with six point DFT $V(k) = \text{Imaginary}[X(k)]$	4
<b>Module 2</b>			
3	(a)	Explain the linear filtering of long data sequences using overlap-save method.	6
	(b)	The 4-point DFT of a real sequence $x(n)$ is $X(k) = (1, j, 1, -j)$ . Find the DFTs of the following. i) $x_1(n) = (-1)^n x(n)$ , ii) $x_2(n) = x((n+1))_4$ , iii) $x_3(n) = x(4-n)$	6
	(c)	Explain the computational complexity of direct computation of DFT. What are the efficient algorithms for the evaluation of the DFT?	4
<b>OR</b>			
4	(a)	Find the response of an LTI system with an impulse response $h(n) = (3,2,1)$ for the input $x(n) = (2, -1, -1, -2, -3, 5,6,-1, 2,0,2,1)$ using overlap and add method. Use 8 point circular convolution.	7
	(b)	The 5-point DFT of a complex sequence $x(n)$ is $X(k)=(j, 1+j, 1+j^2, 4+j)$ . Compute $Y(k)$ , if $y(n)=x^*(n)$ .	4
	(c)	State and prove the property of circular time shift of a sequence.	5
<b>Module 3</b>			

5	(a)	Derive the radix-2 decimation in time FFT algorithm and draw the signal flow graph for eight point DFT computation.	8
	(b)	Find the number of complex additions and complex multiplications required for 128-point DFT computation using i) Direct method, ii) FFT method. What is the speed improvement factor?	3
	(c)	Find the 4-point real sequence $x(n)$ , if its DFT samples are $X(0)=6$ , $X(1)=-2+j2$ , $X(2)=-2$ . Use DIF-FFT algorithm.	5
<b>OR</b>			
6	(a)	Compute the eight point DFT of the sequence $x(n) = \{ \frac{1}{2}, \frac{1}{2}, \frac{1}{2}, \frac{1}{2}, 0, 0, 0, 0 \}$ using the in-place radix-2 decimation in frequency FFT algorithm.	8
	(b)	Explain the Goertzel algorithm and obtain the direct form II realization.	8
<b>Module 4</b>			
7	(a)	Obtain the cascade realization for a system described by $H(z) = \frac{1 + \frac{1}{4}z^{-1}}{\left(1 + \frac{1}{2}z^{-1}\right)\left(1 + \frac{1}{2}z^{-1} + \frac{1}{4}z^{-2}\right)}$ .	5
	(b)	Explain the design of IIR filter by Impulse invariance technique.	6
	(c)	Determine the order and cut off frequency of Butterworth analog highpass filter to meet the specifications: Maximum passband attenuation = 2 dB, Minimum stop band attenuation = 20 dB, Passband edge frequency = 200 rad/sec, stopband edge frequency = 100 rad/sec.	5
<b>OR</b>			
8	(a)	Obtain the parallel realization of the system function $H(z) = \frac{(1+z^{-1})(1+2z^{-1})}{\left(1 + \frac{1}{2}z^{-1}\right)\left(1 - \frac{1}{2}z^{-1}\right)\left(1 + \frac{1}{8}z^{-1}\right)}$	6
	(b)	Design a digital low pass Butterworth filter using bilinear transformation to meet the specifications: i) -3 dB cut-off frequency at $0.5 \pi$ rad, ii) -15 dB at $0.75\pi$ rad. Obtain $H(Z)$ assuming $T=1$ sec.	6
	(c)	What are the characteristics of Chebyshev filters? Define its magnitude response and list the properties of polynomial for type I Chebyshev filters.	4
<b>Module 5</b>			
9	(a)	Realize the linear phase FIR filter for the impulse response $h(n) = \delta(n) + \frac{1}{4} \delta(n-1) - \frac{1}{2} \delta(n-1) + \frac{1}{4} \delta(n-3) + \delta(n-4)$ using direct form.	3
	(b)	Describe the frequency sampling realization of FIR filter.	7
	(c)	Determine the filter coefficients of an FIR filter for the desired frequency response $H_d(\omega) = \begin{cases} e^{-j2\omega}, &  \omega  < \frac{\pi}{4} \\ 0, & \frac{\pi}{4} <  \omega  \leq \pi \end{cases}$ Use rectangular window function. Find the frequency response $H(\omega)$ of the filter.	6
<b>OR</b>			
10	(a)	Consider an FIR lattice filter with coefficients $K_1=0.65$ , $K_2=-0.34$ and $K_3=0.8$ . Find its impulse response and draw the direct form structure.	7
	(b)	Determine the impulse response of an FIR filter to meet the specifications: Passband edge frequency of 1.5 KHz, Stopband edge frequency of 2 KHz, Sampling frequency of 8 KHz. Use the Hamming window function.	6
	(c)	Compare the different window functions used in FIR filter design.	3